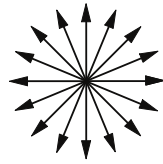
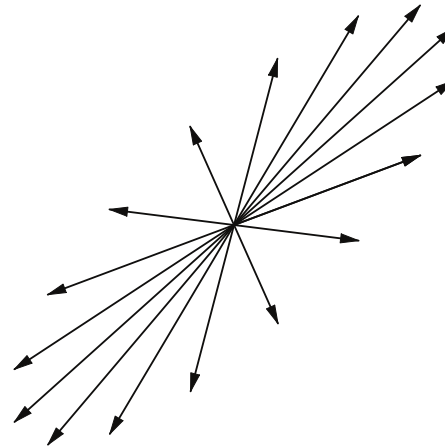


Figure 6.1: (a) The canonical basis vectors  $\mathbf{e}_1$  and  $\mathbf{e}_2$  of  $\mathbb{R}^2$ .  
(b) The images  $\mathbf{a}_1 = \mathbf{A}\mathbf{e}_1$  and  $\mathbf{a}_2 = \mathbf{A}\mathbf{e}_2$  under the matrix  $\mathbf{A}$  given in (6.48).

$$\mathbf{A} = \begin{pmatrix} 3 & 2 \\ 2 & 6 \end{pmatrix}$$



(a)



(b)

Figure 6.2: (a) A set of vectors of unit length; angular interval =  $\pi/8$ .  
(b) The images of the vectors in (a) under the matrix  $\mathbf{A}$  given in (6.48).

$$\mathbf{A} = \begin{pmatrix} 3 & 2 \\ 2 & 6 \end{pmatrix}$$

# MATRIX MULTIPLICATION

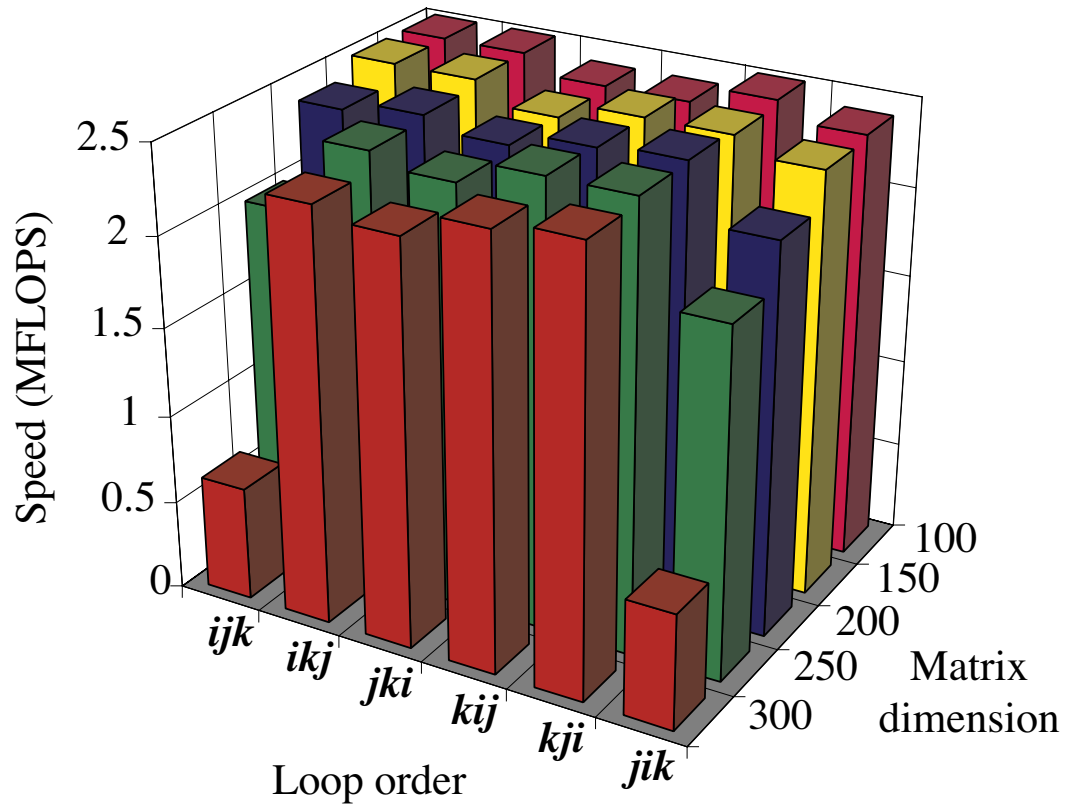


Figure 6.3: Performance of IEEE-754 double-precision FORTRAN matrix multiplication versus matrix size and loop ordering. Cache sizes: Level 1: 32 kB; Level 2: 512 kB.

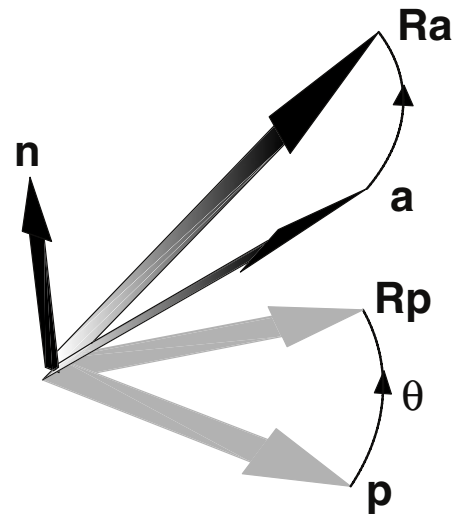


Figure 6.4: Finite rotation of a vector  $\mathbf{a}$  about an axis  $\mathbf{n}$ . The angle of rotation is  $\theta$ . The image of  $\mathbf{a}$  under the rotation is  $\mathbf{Ra}$ . The orthogonal projections  $\mathbf{p}$  and  $\mathbf{Rp}$  of  $\mathbf{a}$  and  $\mathbf{Ra}$  on the plane perpendicular to  $\mathbf{n}$  are shown as shadows.

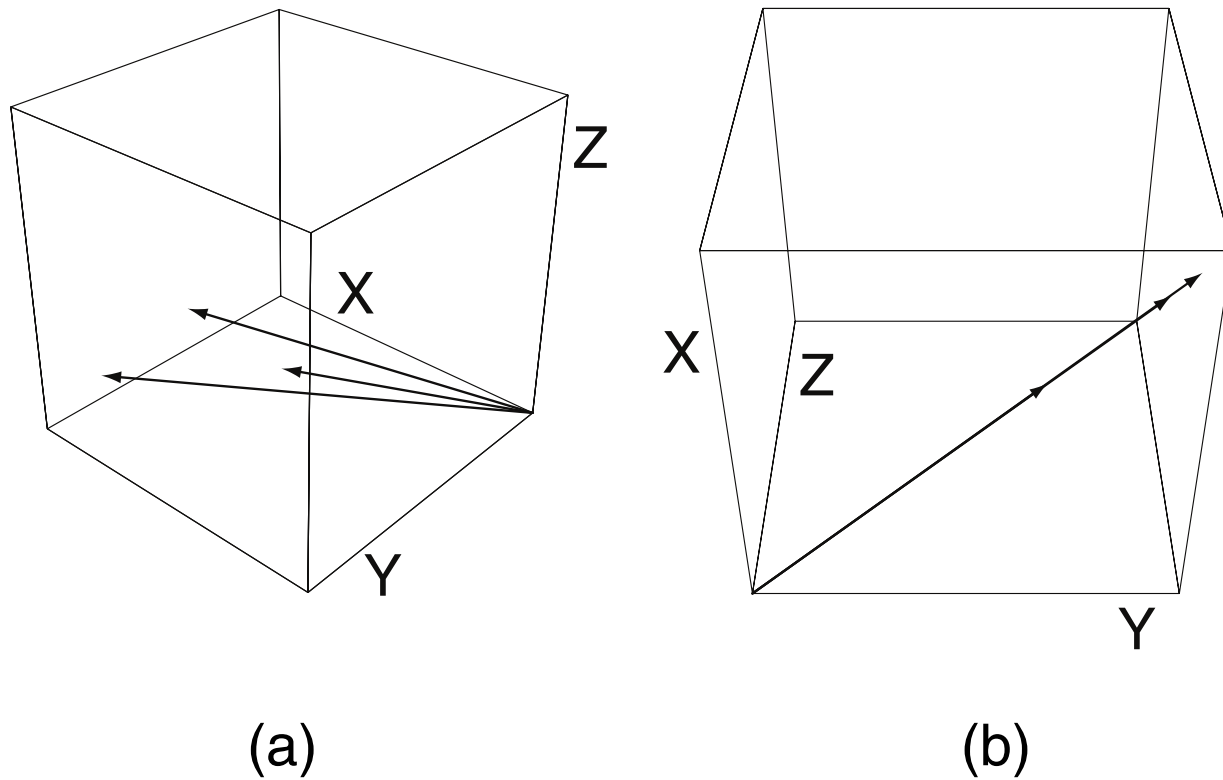


Figure 6.5: (a) Perspective view showing the three column vectors of the matrix  $\mathbf{B}$  defined in Eq. (6.54). (b) Rotated view showing that the vectors lie in a common plane.

$$\mathbf{B} = \begin{pmatrix} 1 & 2 & 1 \\ 2 & 3 & 3 \\ 1 & 1 & 2 \end{pmatrix}$$

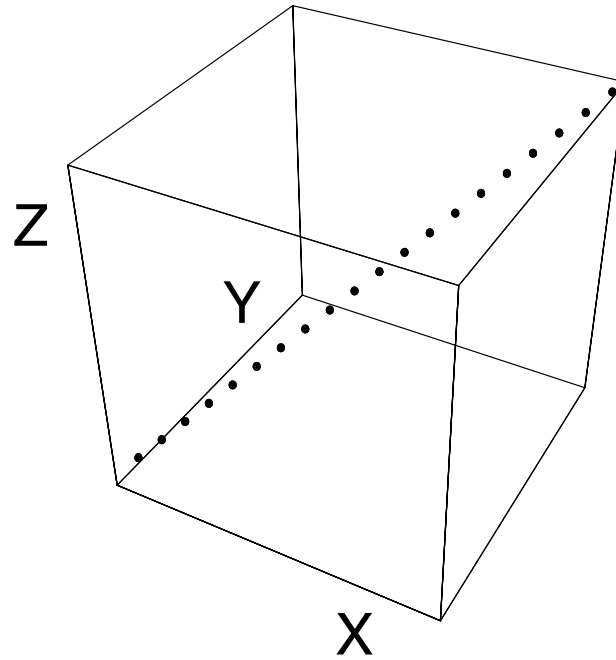


Figure 6.6: The column vectors  $\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_{20}$  of the matrix  $\mathbf{A}$ , plotted as points in three-dimensional space. The point closest to the lower left-hand corner of the bounding box corresponds to the vector  $\mathbf{a}_1$ .

$$\mathbf{A} = (\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_{20}) = \begin{pmatrix} 1 & 4 & \cdots & 3n - 2 & \cdots & 58 \\ 2 & 5 & \cdots & 3n - 1 & \cdots & 59 \\ 3 & 6 & \cdots & 3n & \cdots & 60 \end{pmatrix}$$

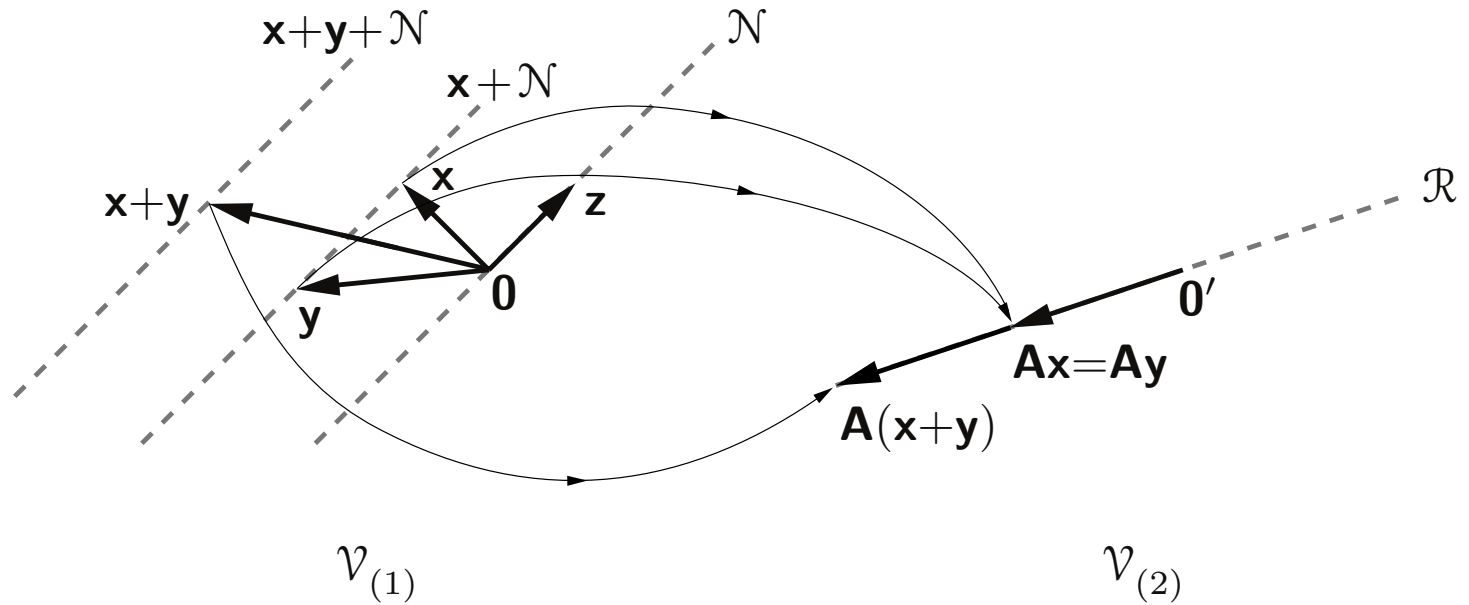


Figure 6.7: Left:  $\mathcal{N}$  is the null space in  $\mathcal{V}_{(1)}$  of the linear mapping  $\mathbf{A}$ . The vectors  $\mathbf{x}$  and  $\mathbf{y}$  belong to the same coset of  $\mathcal{N}$ . Right:  $\mathcal{R}$  is the range of  $\mathbf{A}$  in  $\mathcal{V}_{(2)}$ . Both  $\mathbf{x}$  and  $\mathbf{y}$  have the same image,  $\mathbf{Ax} = \mathbf{Ay}$ .

$$\mathbf{A} = \begin{pmatrix} 1 & -1 \\ \frac{1}{3} & -\frac{1}{3} \end{pmatrix}$$