February 22, 2017 Midterm Exam I EE/TE 4367: Telecommunications Networks

NOTE: Please, complete the following table and keep record of your assignment number.

First Name	
Last Name	
Student ID	
Assignment $\#$	0

Exercise 1. Consider the open network (referred to as the system) of three queues, i.e., Q_1 , Q_2 , and Q_3 , at steady state. New customers arrive at rate λ . A new customer chooses to enter Q_1 with probability p_1 , Q_2 with probability p_2 , and Q_3 with probability $p_3 = 1 - p_1 - p_2$. Customers leaving Q_1 choose to enter Q_2 . Customers leaving Q_2 choose to enter Q_3 . Customers leaving Q_3 choose to either depart from the system with probability q or (re)enter Q_1 with probability 1 - q. The average time spent by a customer in Q_1 while visiting this queue once is T_1 . The average time spent by a customer in Q_2 while visiting this queue once is T_2 . The average time spent by a customer in Q_3 while visiting this queue once is T_3 .

- A) Compute N_1 , N_2 , and N_3 , defined as the average number of customers in Q_1 , Q_2 , and Q_3 , respectively [pt. 10].
- **B)** Compute T, defined as the average total time spent in the system by a customer [pt. 10].
- C) Compute the value of p_3 that would minimize T [pt. 10].

Exercise 2. An Ethernet switch transmits frames at a transmission rate of 10 gigabit per second (Gbps). The frame average length is 900 bytes. The transmitter utilization is 20%. The average number of frames stored in the switch (including the one in transmission) is estimated to be 150.

- A) Compute X, defined as the frame average transmission time [pt. 10].
- **B)** Compute T, defined as the average time a frame spends in the switch at steady-state (T includes both waiting and transmission time) [pt. 10].

Exercise 3. The following string of 7 data bits is transmitted (from left to right) "1110111". A CRC is attached at the end of the string during transmission. The CRC is computed using the generator polynomial $g(D) = D^4 + D^2 + D + 1$.

- A) Compute c(D), defined as the remainder when $D^4s(D)$ is divided by g(D), using modulo 2 arithmetic, where s(D) is the polynomial representing the string of data bits. Write down the sequence of bits as they are transmitted inclusive of CRC, starting left with the first bit to be transmitted [pt. 10].
- B) Assume that at the receiver the sequence of bits is affected by an error, described by $e(D) = D^{10} + D^3$. Compute r(D), defined as the remainder when $D^3s(D) + c(D) + e(D)$ is divided by g(D), using modulo 2 arithmetic. Is the error detected by the receiver, and if so, why [pt. 10]?