

Chapter 3: National Income: Where it Comes From and Where it Goes

CHAPTER 3 National Income

0

Outline of model

A closed economy, market-clearing model

- Supply side
 - factor markets (supply, demand, price)
 - determination of output/income
- Demand side
 - determinants of C, I, and G
- Equilibrium
 - goods market
 - loanable funds market

CHAPTER 3 National Income

1

Factors of production

K = capital:
tools, machines, and structures used in production

L = labor:
the physical and mental efforts of workers

CHAPTER 3 National Income

2

The production function: $Y = F(K,L)$

- shows how much output (**Y**) the economy can produce from **K** units of capital and **L** units of labor
- reflects the economy's level of technology
- exhibits constant returns to scale

CHAPTER 3 National Income

3

Returns to scale: A review

Initially $Y_1 = F(K_1, L_1)$

Scale all inputs by the same factor **z**:

$$K_2 = zK_1 \text{ and } L_2 = zL_1$$

(e.g., if $z = 1.2$, then all inputs are increased by 20%)

What happens to output, $Y_2 = F(K_2, L_2)$?

- If **constant returns to scale**, $Y_2 = zY_1$
- If **increasing returns to scale**, $Y_2 > zY_1$
- If **decreasing returns to scale**, $Y_2 < zY_1$

CHAPTER 3 National Income

4

Returns to scale: Example 1

$$F(K,L) = \sqrt{KL}$$

$$F(zK, zL) = \sqrt{(zK)(zL)}$$

$$= \sqrt{z^2 KL}$$

$$= \sqrt{z^2} \sqrt{KL}$$

$$= z\sqrt{KL}$$

$$= zF(K,L)$$

constant returns to scale for any $z > 0$

CHAPTER 3 National Income

5

Returns to scale: Example 2

$$F(K,L) = \sqrt{K} + \sqrt{L}$$

$$F(zK, zL) = \sqrt{zK} + \sqrt{zL}$$

$$= \sqrt{z}\sqrt{K} + \sqrt{z}\sqrt{L}$$

$$= \sqrt{z}(\sqrt{K} + \sqrt{L})$$

$$= \sqrt{z}F(K,L)$$

*decreasing
returns to scale
for any $z > 1$*

Returns to scale: Example 3

$$F(K,L) = K^2 + L^2$$

$$F(zK, zL) = (zK)^2 + (zL)^2$$

$$= z^2(K^2 + L^2)$$

$$= z^2 F(K,L)$$

*increasing returns
to scale for any
 $z > 1$*

NOW YOU TRY:**Returns to Scale**

- Determine whether each of these production functions has constant, decreasing, or increasing returns to scale:

(a) $F(K,L) = \frac{K^2}{L}$

(b) $F(K,L) = K + L$

NOW YOU TRY:**Answers, part (a)**

$$F(K,L) = \frac{K^2}{L}$$

$$F(zK, zL) = \frac{(zK)^2}{zL} = \frac{z^2 K^2}{zL} = z \frac{K^2}{L} = zF(K,L)$$

*constant returns to
scale for any $z > 0$*

NOW YOU TRY:**Answers, part (b)**

$$F(K,L) = K + L$$

$$F(zK, zL) = zK + zL$$

$$= z(K + L)$$

$$= zF(K,L) \quad \text{constant returns to scale for any } z > 0$$

Assumptions

- Technology is fixed.
- The economy's supplies of capital and labor are fixed at

$$K = \bar{K} \quad \text{and} \quad L = \bar{L}$$

Determining GDP

Output is determined by the fixed factor supplies and the fixed state of technology:

$$\bar{Y} = F(\bar{K}, \bar{L})$$

CHAPTER 3 National Income

12

The distribution of national income

- determined by **factor prices**, the prices per unit firms pay for the factors of production
 - wage = price of L
 - **rental rate** = price of K

CHAPTER 3 National Income

13

Notation

W	= nominal wage
R	= nominal rental rate
P	= price of output
W/P	= real wage (measured in units of output)
R/P	= real rental rate

CHAPTER 3 National Income

14

How factor prices are determined

- Factor prices are determined by supply and demand in factor markets.
- Recall: Supply of each factor is fixed.
- What about demand?

CHAPTER 3 National Income

15

Demand for labor

- Assume markets are competitive: each firm takes W , R , and P as given.
- Basic idea: A firm hires each unit of labor if the cost does not exceed the benefit.
 - cost = real wage
 - benefit = marginal product of labor

CHAPTER 3 National Income

16

Marginal product of labor (MPL)

- definition: The extra output the firm can produce using an additional unit of labor (holding other inputs fixed):

$$MPL = F(K, L+1) - F(K, L)$$

CHAPTER 3 National Income

17

NOW YOU TRY:
Compute & graph MPL

a. Determine **MPL** at each value of **L**.
 b. Graph the production function.
 c. Graph the **MPL** curve with **MPL** on the vertical axis and **L** on the horizontal axis.

L	Y	MPL
0	0	n.a.
1	10	?
2	19	?
3	27	8
4	34	?
5	40	?
6	45	?
7	49	?
8	52	?
9	54	?
10	55	?

NOW YOU TRY:
Answers

Production function

Marginal Product of Labor

MPL and the production function

CHAPTER 3 National Income 20

Diminishing marginal returns

- As a factor input is increased, its marginal product falls (other things equal).
- Intuition:
 Suppose $\uparrow L$ while holding K fixed
 \Rightarrow fewer machines per worker
 \Rightarrow lower worker productivity

CHAPTER 3 National Income 21

NOW YOU TRY:
Identifying Diminishing Marginal Returns

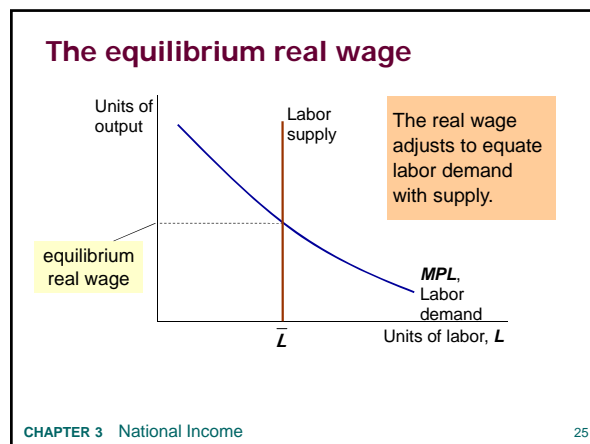
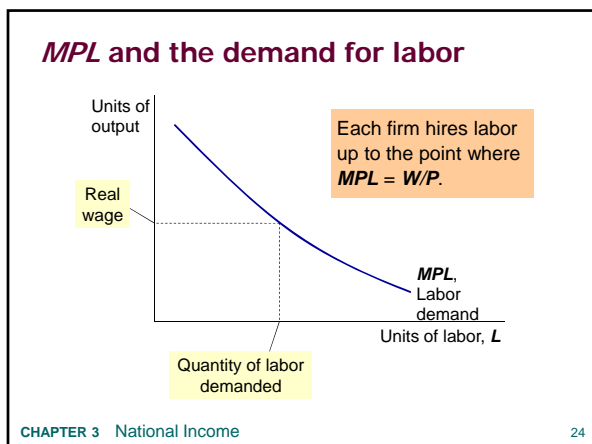
- Which of these production functions have diminishing marginal returns to labor?
 - $F(K, L) = 2K + 15L$
 - $F(K, L) = \sqrt{KL}$
 - $F(K, L) = 2\sqrt{K} + 15\sqrt{L}$

NOW YOU TRY:
MPL and labor demand

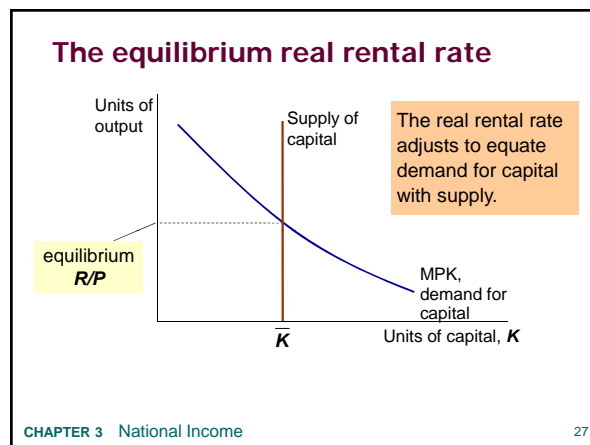
Suppose $W/P = 6$.

- If $L = 3$, should firm hire more or less labor? Why?
- If $L = 7$, should firm hire more or less labor? Why?

L	Y	MPL
0	0	n.a.
1	10	10
2	19	9
3	27	8
4	34	7
5	40	6
6	45	5
7	49	4
8	52	3
9	54	2
10	55	1



- ### Determining the rental rate
- We have just seen that $MPL = W/P$.
 - The same logic shows that $MPK = R/P$:
 - diminishing returns to capital: $MPK \downarrow$ as $K \uparrow$
 - The MPK curve is the firm's demand curve for renting capital.
 - Firms maximize profits by choosing K such that $MPK = R/P$.
- CHAPTER 3 National Income 26



- ### The Neoclassical Theory of Distribution
- states that each factor input is paid its marginal product
 - a good starting point for thinking about income distribution
- CHAPTER 3 National Income 28

How income is distributed to L and K

$$\text{total labor income} = \frac{W}{P} \bar{L} = MPL \times \bar{L}$$

$$\text{total capital income} = \frac{R}{P} \bar{K} = MPK \times \bar{K}$$

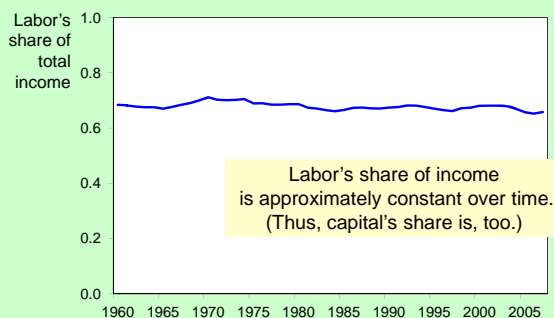
If production function has constant returns to scale, then

$$\bar{Y} = \underbrace{MPL \times \bar{L}}_{\text{labor income}} + \underbrace{MPK \times \bar{K}}_{\text{capital income}}$$

national income

CHAPTER 3 National Income 29

The ratio of labor income to total income in the U.S., 1960-2007



The Cobb-Douglas Production Function

- The Cobb-Douglas production function has constant factor shares:

α = capital's share of total income:

$$\text{capital income} = MPK \times K = \alpha Y$$

$$\text{labor income} = MPL \times L = (1 - \alpha)Y$$

- The Cobb-Douglas production function is:

$$Y = AK^\alpha L^{1-\alpha}$$

where A represents the level of technology.

CHAPTER 3 National Income

31

The Cobb-Douglas Production Function

- Each factor's marginal product is proportional to its average product:

$$MPK = \alpha AK^{\alpha-1} L^{1-\alpha} = \frac{\alpha Y}{K}$$

$$MPL = (1 - \alpha) AK^\alpha L^{-\alpha} = \frac{(1 - \alpha)Y}{L}$$

CHAPTER 3 National Income

32

Labor productivity and wages

- Theory: wages depend on labor productivity
- U.S. data:

period	productivity growth	real wage growth
1959-2007	2.1%	2.0%
1959-1973	2.8%	2.8%
1973-1995	1.4%	1.2%
1995-2007	2.5%	2.4%

CHAPTER 3 National Income

33

Outline of model

A closed economy, market-clearing model

Supply side

DONE ✓ factor markets (supply, demand, price)

DONE ✓ determination of output/income

Demand side

Next → □ determinants of C , I , and G

Equilibrium

□ goods market

□ loanable funds market

CHAPTER 3 National Income

34

Demand for goods & services

Components of aggregate demand:

C = consumer demand for g & s

I = demand for investment goods

G = government demand for g & s

(closed economy: no NX)

CHAPTER 3 National Income

35

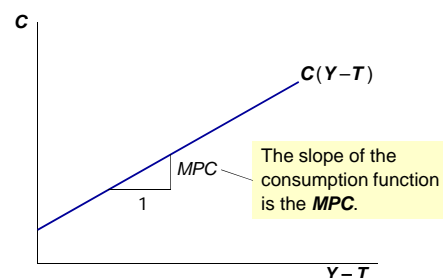
Consumption, C

- def: **Disposable income** is total income minus total taxes: $Y - T$.
- Consumption function: $C = C(Y - T)$
Shows that $\uparrow(Y - T) \Rightarrow \uparrow C$
- def: **Marginal propensity to consume (MPC)** is the change in C when disposable income increases by one dollar.

CHAPTER 3 National Income

36

The consumption function



CHAPTER 3 National Income

37

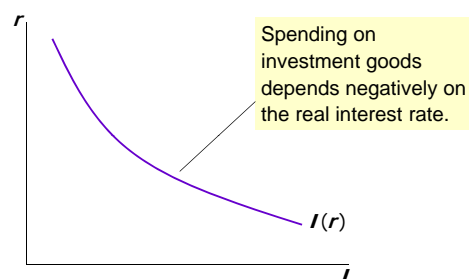
Investment, I

- The investment function is $I = I(r)$, where r denotes the **real interest rate**, the nominal interest rate corrected for inflation.
 - The real interest rate is
 - the cost of borrowing
 - the opportunity cost of using one's own funds to finance investment spending
- So, $\uparrow r \Rightarrow \downarrow I$

CHAPTER 3 National Income

38

The investment function



CHAPTER 3 National Income

39

Government spending, G

- G = govt spending on goods and services.
- G excludes transfer payments (e.g., social security benefits, unemployment insurance benefits).
- Assume government spending and total taxes are exogenous:

$$G = \bar{G} \quad \text{and} \quad T = \bar{T}$$

CHAPTER 3 National Income

40

The market for goods & services

- Aggregate demand: $C(\bar{Y} - \bar{T}) + I(r) + \bar{G}$
- Aggregate supply: $\bar{Y} = F(\bar{K}, \bar{L})$
- Equilibrium: $\bar{Y} = C(\bar{Y} - \bar{T}) + I(r) + \bar{G}$

The real interest rate adjusts to equate demand with supply.

CHAPTER 3 National Income

41

The loanable funds market

- A simple supply-demand model of the financial system.
- One asset: “loanable funds”
 - demand for funds: investment
 - supply of funds: saving
 - “price” of funds: real interest rate

CHAPTER 3 National Income

42

Demand for funds: Investment

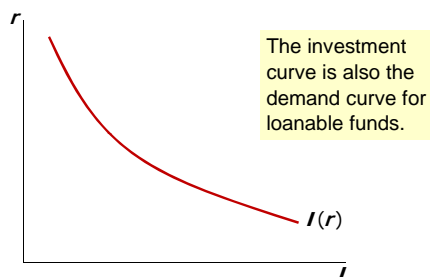
The demand for loanable funds...

- comes from investment:
Firms borrow to finance spending on plant & equipment, new office buildings, etc.
Consumers borrow to buy new houses.
- depends negatively on r ,
the “price” of loanable funds
(cost of borrowing).

CHAPTER 3 National Income

43

Loanable funds demand curve



CHAPTER 3 National Income

44

Supply of funds: Saving

- The supply of loanable funds comes from saving:
 - Households use their saving to make bank deposits, purchase bonds and other assets. These funds become available to firms to borrow to finance investment spending.
 - The government may also contribute to saving if it does not spend all the tax revenue it receives.

CHAPTER 3 National Income

45

Types of saving

$$\text{private saving} = (Y - T) - C$$

$$\text{public saving} = T - G$$

national saving, S

= private saving + public saving

$$= (Y - T) - C + T - G$$

$$= Y - C - G$$

CHAPTER 3 National Income

46

Notation: Δ = change in a variable

- For any variable X , ΔX = “the change in X ”
 Δ is the Greek (uppercase) letter *Delta*

Examples:

- If $\Delta L = 1$ and $\Delta K = 0$, then $\Delta Y = MPL$.
More generally, if $\Delta K = 0$, then $MPL = \frac{\Delta Y}{\Delta L}$.
- $\Delta(Y - T) = \Delta Y - \Delta T$, so

$$\Delta C = MPC \times (\Delta Y - \Delta T)$$

$$= MPC \Delta Y - MPC \Delta T$$

CHAPTER 3 National Income

47

NOW YOU TRY:
Calculate the change in saving

Suppose $MPC = 0.8$ and $MPL = 20$.
 For each of the following, compute ΔS :

- a. $\Delta G = 100$
- b. $\Delta T = 100$
- c. $\Delta Y = 100$
- d. $\Delta L = 10$

NOW YOU TRY:
Answers

$$\Delta S = \Delta Y - \Delta C - \Delta G = \Delta Y - 0.8(\Delta Y - \Delta T) - \Delta G$$

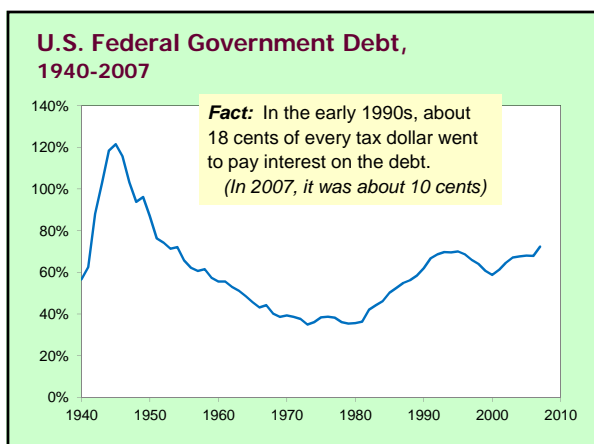
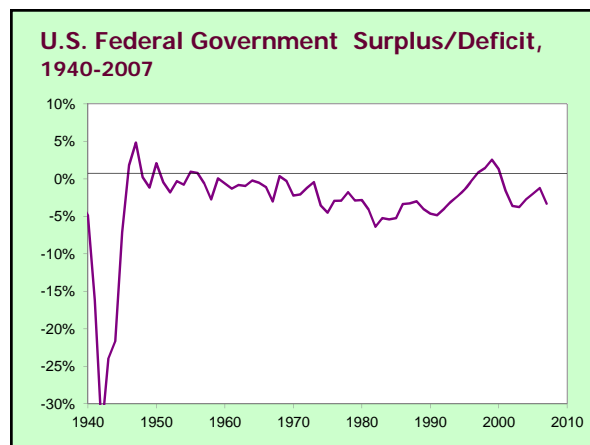
$$= 0.2\Delta Y + 0.8\Delta T - \Delta G$$

- a. $\Delta S = -100$
- b. $\Delta S = 0.8 \times 100 = 80$
- c. $\Delta S = 0.2 \times 100 = 20$
- d. $\Delta Y = MPL \times \Delta L = 20 \times 10 = 200$,
 $\Delta S = 0.2 \times \Delta Y = 0.2 \times 200 = 40$.

Budget surpluses and deficits

- If $T > G$, **budget surplus** = $(T - G)$
 = public saving.
- If $T < G$, **budget deficit** = $(G - T)$
 and public saving is negative.
- If $T = G$, "balanced budget," public saving = 0.
- The U.S. government finances its deficit by issuing Treasury bonds – *i.e.*, borrowing.

CHAPTER 3 National Income 50

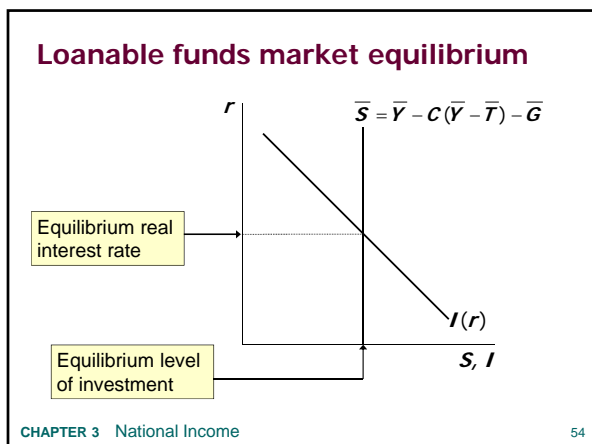


Loanable funds supply curve

$$\bar{S} = \bar{Y} - c(\bar{Y} - \bar{T}) - \bar{G}$$

National saving does not depend on r , so the supply curve is vertical.

CHAPTER 3 National Income 53



The special role of r

r adjusts to equilibrate the goods market and the loanable funds market simultaneously:

If L.F. market in equilibrium, then

$$Y - C - G = I$$

Add $(C + G)$ to both sides to get

$$Y = C + I + G \text{ (goods market eq'm)}$$

Thus,

Eq'm in L.F. market \Leftrightarrow Eq'm in goods market

CHAPTER 3 National Income 55

Digression: Mastering models

To master a model, be sure to know:

1. Which of its variables are endogenous and which are exogenous.
2. For each curve in the diagram, know:
 - a. definition
 - b. intuition for slope
 - c. all the things that can shift the curve
3. Use the model to analyze the effects of each item in 2c.

CHAPTER 3 National Income 56

Mastering the loanable funds model

Things that shift the saving curve

- public saving
 - fiscal policy: changes in G or T
- private saving
 - preferences
 - tax laws that affect saving
 - 401(k)
 - IRA
 - replace income tax with consumption tax

CHAPTER 3 National Income 57

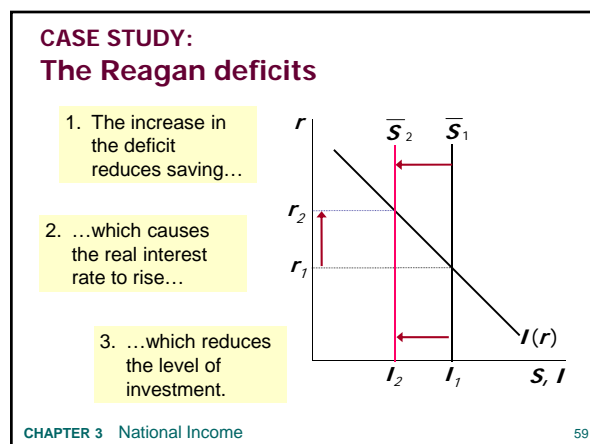
CASE STUDY: The Reagan deficits

- Reagan policies during early 1980s:
 - increases in defense spending: $\Delta G > 0$
 - big tax cuts: $\Delta T < 0$
- Both policies reduce national saving:

$$\bar{S} = \bar{Y} - C(\bar{Y} - \bar{T}) - \bar{G}$$

$\uparrow \bar{G} \Rightarrow \downarrow \bar{S}$ $\downarrow \bar{T} \Rightarrow \uparrow C \Rightarrow \downarrow \bar{S}$

CHAPTER 3 National Income 58



Are the data consistent with these results?

variable	1970s	1980s
$T - G$	-2.2	-3.9
S	19.6	17.4
r	1.1	6.3
I	19.9	19.4

*T-G, S, and I are expressed as a percent of GDP
All figures are averages over the decade shown.*

NOW YOU TRY:

The effects of saving incentives

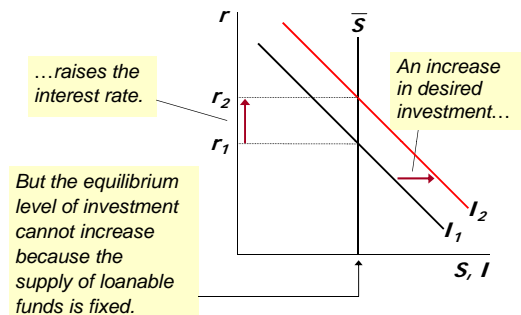
- Draw the diagram for the loanable funds model.
- Suppose the tax laws are altered to provide more incentives for private saving. (Assume that total tax revenue T does not change)
- What happens to the interest rate and investment?

Mastering the loanable funds model, continued

Things that shift the investment curve:

- some technological innovations
 - to take advantage some innovations, firms must buy new investment goods
- tax laws that affect investment
 - e.g., investment tax credit

An increase in investment demand

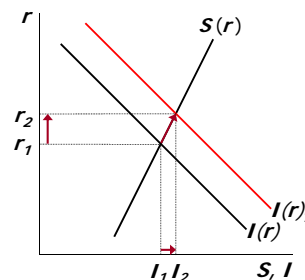


Saving and the interest rate

- Why might saving depend on r ?
- How would the results of an increase in investment demand be different?
 - Would r rise as much?
 - Would the equilibrium value of I change?

An increase in investment demand when saving depends on r

An increase in investment demand raises r , which induces an increase in the quantity of saving, which allows I to increase.



FYI: Markets, Intermediaries, the 2008 Crisis

- In the real world, firms have several options for raising funds they need for investment, including:
 - borrow from banks
 - sell bonds to savers
 - sell shares of stock (ownership) to savers
- The financial system includes:
 - bond and stock markets, where savers *directly* provide funds to firms for investment
 - financial intermediaries, e.g. banks, insurance companies, mutual funds, where savers *indirectly* provide funds to firms for investment

CHAPTER 3 National Income

66

FYI: Markets, Intermediaries, the 2008 Crisis

- Intermediaries can help move funds to their most productive uses.
- But when intermediaries are involved, savers usually do not know what investments their funds are financing.
- Intermediaries were at the heart of the financial crisis of 2008....

CHAPTER 3 National Income

67

FYI: Markets, Intermediaries, the 2008 Crisis

A few details on the financial crisis:

- July '06 to Dec '08: house prices fell 27%
- Jan '08 to Dec '08: 2.3 million foreclosures
- Many banks, financial institutions holding mortgages or mortgage-backed securities driven to near bankruptcy
- Congress authorized \$700 billion to help shore up financial institutions

CHAPTER 3 National Income

68

Chapter Summary

- Total output is determined by:
 - the economy's quantities of capital and labor
 - the level of technology
- Competitive firms hire each factor until its marginal product equals its price.
- If the production function has constant returns to scale, then labor income plus capital income equals total income (output).

Chapter Summary

- A closed economy's output is used for:
 - consumption
 - investment
 - government spending
- The real interest rate adjusts to equate the demand for and supply of:
 - goods and services
 - loanable funds

Chapter Summary

- A decrease in national saving causes the interest rate to rise and investment to fall.
- An increase in investment demand causes the interest rate to rise, but does not affect the equilibrium level of investment if the supply of loanable funds is fixed.