MATH 2415 Paper Hwk on Lines and Planes (12.5)

Recall the following definitions:

- (i) A vector parametrization of the line through the endpoint of the vector \mathbf{a} in the direction of the vector \mathbf{b} is given by $\mathbf{r}(t) = \mathbf{a} + t\mathbf{b}$, where $t \in \mathbf{R}$.
- (ii) A scalar parametrization of the line in (i) is

$$x = a_1 + tb_1$$
$$y = a_2 + tb_2$$
$$z = a_3 + tb_3$$

where $\mathbf{a} = (a_1, a_2, a_3)$ and $\mathbf{b} = (b_1, b_2, b_3)$.

- (iii) A level set equation of a plane is an equation of the form ax + by + cz = d, where a, b, c, d are real numbers.
- (iv) A **parametrization** of a plane through the endpoint of the vector **u** that contains the vectors **v** and **w** is of the form $\mathbf{r}(s,t) = \mathbf{u} + s\mathbf{v} + t\mathbf{w}$, where $s, t \in \mathbf{R}$.

(1) Find a vector parametrization for the line passing through the points (1, 2, 3) and (9, 8, 7).

(2) Find the level set equation and a parametrization of the plane through the point (1, 2, 3) with normal vector (4, 5, 6).

(3) Find the level set equation of the plane through the point (1, 2, 3) parallel to the plane 3x - 5y + 7z = 8.

(4) Find the level set equation and a parametrization of the plane through the points (1, 0, -1), (3, 3, 2), and (4, 5, -1).

(5) Find a parametrization of the plane that contains both the point (2, 4, 6) and the line x = 7 - 3t, y = 3 + 4t, z = 5 + 2t.

(6) Does the line x = 3 + 2t, y = 6 - 5t, z = 2 + 3t intersect the plane 3x + 2y - 4z = 1?